

## Calculus: Day-wise Lesson Plan

Teacher: Krishan Sharma

Course: B.Sc. I Sem (As per NEP 2020) Subject: Calculus

Duration: 45 Days (Theory) + 30 Days (Practical)

### Theory Plan (45 Days)

| Day    | Topic                                                                                             |
|--------|---------------------------------------------------------------------------------------------------|
| Day 1  | Course introduction, syllabus, assessment pattern. Intro to limits — intuitive idea and examples. |
| Day 2  | Basic properties of limits and limit laws. Practice problems.                                     |
| Day 3  | $\epsilon$ - $\delta$ definition of limit — formal definition and worked examples.                |
| Day 4  | Continuity: definitions, examples, and continuous functions.                                      |
| Day 5  | Types of discontinuities (removable, jump, infinite) and examples.                                |
| Day 6  | Differentiability: definition, geometric meaning, and examples.                                   |
| Day 7  | Rules of differentiation (product, quotient, chain) with practice.                                |
| Day 8  | L'Hospital's rule — statement, proof sketch, and applications.                                    |
| Day 9  | Successive differentiation — higher derivatives and examples.                                     |
| Day 10 | Leibniz theorem for nth derivative of a product — statement and problems.                         |
| Day 11 | Taylor series — concept, expansion for standard functions, radius of convergence.                 |
| Day 12 | Maclaurin series, remainder forms and examples.                                                   |
| Day 13 | Unit I Test (short written problems + problem solving).                                           |
| Day 14 | Test feedback, common mistakes, and remedial practice (Unit I).                                   |
| Day 15 | Unit II — Introduction to asymptotes; horizontal & vertical asymptotes (algebraic curves).        |
| Day 16 | Oblique asymptotes and methods to find them (algebraic curves).                                   |
| Day 17 | Asymptotes for polar curves and examples.                                                         |
| Day 18 | Intersection of a curve and its asymptotes; worked problems.                                      |
| Day 19 | Curvature: geometric idea; curvature and radius of curvature (Cartesian form).                    |
| Day 20 | Curvature in parametric and polar forms; examples and computation techniques.                     |

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| Day 21 | Newton's method — derivation, convergence discussion and examples.                   |
| Day 22 | Centre of curvature and circle of curvature — definitions and examples.              |
| Day 23 | Problem solving session: asymptotes & curvature combined problems.                   |
| Day 24 | Unit II Test (written + applications problems).                                      |
| Day 25 | Test feedback & remedial practice (Unit II).                                         |
| Day 26 | Unit III — Multiple points: definitions, identification and simple examples.         |
| Day 27 | Classification of multiple points: node, cusp, conjugate point, with examples.       |
| Day 28 | Tests for concavity and convexity; second derivative test and examples.              |
| Day 29 | Points of inflection — identification and worked problems.                           |
| Day 30 | Tracing curves — Cartesian coordinate methods (step-by-step procedure).              |
| Day 31 | Tracing curves — Parametric form (method + examples).                                |
| Day 32 | Tracing curves — Polar form (method + examples).                                     |
| Day 33 | Reduction formulae — introduction and derivation for common integrals.               |
| Day 34 | Reduction formulae — problems and recursive techniques.                              |
| Day 35 | Curve tracing & reduction formulae intensive problem-solving session.                |
| Day 36 | Unit III Test (written + curve tracing problems).                                    |
| Day 37 | Test feedback & remedial practice (Unit III).                                        |
| Day 38 | Unit IV — Rectification and arc length for Cartesian curves (derivation + examples). |
| Day 39 | Arc length for parametric and polar curves; sample problems.                         |
| Day 40 | Intrinsic equation of a curve and quadrature — concepts and examples.                |
| Day 41 | Area bounded by closed curves — methods and examples.                                |
| Day 42 | Volumes of solids of revolution — disk/washer and shell methods (Cartesian).         |
| Day 43 | Surfaces of revolution — surface area formulae and examples (parametric & polar).    |
| Day 44 | Mixed problem-solving session (Units III & IV) — integrated problems and revision.   |
| Day 45 | Final Theory Test (comprehensive; covers Units I–IV).                                |

### Practical Plan (30 Days)

| Practical Day | Topic                                                                                |
|---------------|--------------------------------------------------------------------------------------|
| Day 1         | Introduction to MAXIMA — interface, basic operators and functions.                   |
| Day 2         | Simplify algebraic expressions and expressions with radicals/logs/trig using MAXIMA. |
| Day 3         | Expand algebraic, rational, trigonometric and logarithmic expressions in MAXIMA.     |
| Day 4         | Compute derivatives (algebraic, trig, exponential, log) with MAXIMA.                 |
| Day 5         | Derivatives of composed functions and chain-rule examples in MAXIMA.                 |
| Day 6         | Successive differentiation problems and verification with MAXIMA.                    |
| Day 7         | Indefinite integrals of various functions using MAXIMA.                              |
| Day 8         | Definite integrals and numerical evaluation in MAXIMA.                               |
| Day 9         | Plotting Cartesian curves using MAXIMA.                                              |
| Day 10        | Plotting parametric curves using MAXIMA.                                             |
| Day 11        | Plotting polar curves using MAXIMA.                                                  |
| Day 12        | Demonstration of singular points (node, cusp) using MAXIMA.                          |
| Day 13        | Curve tracing (Cartesian) using MAXIMA.                                              |
| Day 14        | Curve tracing (Parametric) using MAXIMA.                                             |
| Day 15        | Curve tracing (Polar) using MAXIMA.                                                  |
| Day 16        | Compute radius of curvature (Cartesian/parametric/polar) using MAXIMA.               |
| Day 17        | Compute length of curves (arc length) using MAXIMA.                                  |
| Day 18        | Volumes & surfaces of revolution using MAXIMA.                                       |
| Day 19        | Manual problem-solving session: successive differentiation & reduction formulae.     |
| Day 20        | Manual problem-solving session: volumes & surface area.                              |
| Day 21        | Mid-practical exam — execute MAXIMA program + solve problem by hand.                 |
| Day 22        | Viva-voce and submission of practical record (midterm submission).                   |
| Day 23        | Advanced plotting/visualization in MAXIMA.                                           |
| Day 24        | Group mini-project: trace a complex curve.                                           |
| Day 25        | Lab assignment: compile MAXIMA program portfolio.                                    |

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| Day 26 | Debugging session: common MAXIMA errors and fixes.        |
| Day 27 | Mock practical exam — run-through under exam conditions.  |
| Day 28 | Practical revision, doubt clearing and record completion. |
| Day 29 | Final practical exam (program + write-up + viva).         |
| Day 30 | Final feedback, grades submission and wrap-up.            |

### Lesson Plan 2025-26

Name of the Assistant Professor: **Ms. Manisha**

Class and Section: **B.Sc. 3<sup>rd</sup> Semester (NEP)**

Subject: **Mathematics (Differential Equations)**

| Week | Date              | Topics                                                                                                                                                               |
|------|-------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1    | 1 Aug- 9Aug       | Introduction to differential equations, solution of differential equations of first order and first degree. Exercise 1.1,1.2,1.3,1.4.                                |
| 2    | 11 Aug- 16 Aug    | Exact DEs, Solution of exact DEs, Integrating factors, exercise 2.1 to 2.4                                                                                           |
| 3    | 18 Aug – 23 Aug   | Exercise 2.5 to 2.7. Solution of equation of first order but not of first degree. Exercise 3.1, 3.2.                                                                 |
| 4    | 25 Aug – 30 Aug   | Exercise 3.3, Lagrange equation, Clairaut's equation, Exc. 3.4, equation reducible to Clairaut's eqn. exc. 3.5.                                                      |
| 5    | 1 Sept – 6 Sept   | Singular solution, Exc. 3.6. Introduction to orthogonal trajectories, problems & exercise 4.1.                                                                       |
| 6    | 8 Sept – 13 Sept  | Introduction to Linear DE with constant coefficient, Solution of homogeneous and non-homogeneous DE, exc. 5.1, 5.2, 5.3.                                             |
| 7    | 15 Sept – 20 Sept | Exercise 5.4 to 5.6, Cauchy-Euler equation, exc. 6.1. Linear DE of second order with variable coeff, exercise 7.1. CLASS TEST                                        |
| 8    | 22 Sept – 27 Sept | Solution of DE of second order by method of variation of parameters, exercise 7.2, solving linear DE of second order by method of undetermined coeff., exercise 7.3. |
| 9    | 29 Sept – 4 Oct   | Solution of Ordinary Simultaneous DE, exc. 8.1, 8.2, second integral found with the help of first, exc. 8.3.                                                         |
| 10   | 6 Oct – 11 Oct    | Introduction to total differential equations, necessary and sufficient condition for integrability of total DE, exercise 9.1, 9.2.                                   |
| 11   | 13 Oct – 18 Oct   | Exercise 9.3, 9.4, Introduction to Partial DEs.                                                                                                                      |
| 12   | 27 Oct- 1 Nov     | Solution of first order linear Partial DEs, exc. 10.1.                                                                                                               |

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| 13 | 03 Nov- 08 Nov | Integral surfaces passing through a curve, Exc. 10.2, surfaces orthogonal to given system of surfaces, Exc. 10.3. Introduction to first order non-linear PDE, Exc. 11.1. |
| 14 | 10 Nov- 15 Nov | Charpit's method, Jacobi's method, Exc. 11.2 to 11.4.                                                                                                                    |
| 15 | 17 Nov- 22 Nov | Second order Linear PDE with const. coeff, solution of homogeneous, non-homogeneous PDE, exc. 12.1, 12.2.                                                                |
| 16 | 24 Nov- 29 Nov | Problem Discussion, Revision                                                                                                                                             |
| 17 | 1 Dec onwards  | EXAMINATIONS                                                                                                                                                             |

## Practical

| Practical Day | Topic                                                                                                            |
|---------------|------------------------------------------------------------------------------------------------------------------|
| 1             | Introduction to MAXIMA — interface, basic operators and functions.                                               |
| 2             | Problems solving for differential equations which are reducible to homogeneous.                                  |
| 3             | Problems solving for differential equations which are Exact differential equations.                              |
| 4             | Problems solving for linear differential equations with constant coefficient.                                    |
| 5             | Problems solving for linear differential equations with variable coefficient.                                    |
| 6             | Problems solving for differential equations by method of variation of parameters.                                |
| 7             | Problems solving for differential equations by method of undetermined coefficients.                              |
| 8             | Problems solving for simultaneous differential equations.                                                        |
| 9             | Problems solving for different PDEs using Lagrange's method.                                                     |
| 10            | Problems solving for PDEs with Charpit's method and Jacobi's method.                                             |
| 11            | Solutions of first and second order differential equations in MAXIMA.                                            |
| 12            | Plotting of family of solutions of differential equations of first, second and third order using MAXIMA.         |
| 13            | Solution of differential equations using method of variation of parameters using MAXIMA.                         |
| 14            | Growth and decay model (exponential case only).                                                                  |
| 15            | Lake pollution model (with constant/seasonal flow and pollution concentration).                                  |
| 16            | Density-dependent growth model.                                                                                  |
| 17            | Predatory-prey model (basic Volterra model, with density dependence, effect of DDT, two prey one predator).      |
| 18            | To find the solutions Linear differential equations of second order using built in functions of MAXIMA software. |
| 19            | To find numerical solution of a first order ODE using plotdf built in function of MAXIMA.                        |
| 20            | To find exact solutions of first and second order ODEs using ode2 and ic1/ic2 built in functions of MAXIMA.      |
| 21            | To find exact solutions of first and second order ODEs using desolve and atvalue built in functions of MAXIMA.   |

Teacher Name: **Krishan Sharma**  
Course: B.Sc. V Sem

## Real Analysis (Paper: 12BSM 351)

### Unit I: The Riemann Integral

| Day       | Topic                                                                                               |
|-----------|-----------------------------------------------------------------------------------------------------|
| Day 1     | Course introduction, syllabus overview, and assessment pattern.                                     |
| Day 2–4   | Partitions of an interval, upper and lower Riemann sums, and related properties.                    |
| Day 5–7   | Definition of the Riemann integral, necessary and sufficient conditions for integrability.          |
| Day 8–10  | Integrability of continuous functions and monotonic functions with proofs and examples.             |
| Day 11–13 | The Fundamental Theorem of Integral Calculus: First and second forms, with proofs and applications. |
| Day 14–16 | Mean Value Theorems of Integral Calculus: First and second Mean Value Theorems with examples.       |
| Day 17–19 | Intensive problem-solving session covering all topics in Unit I.                                    |
| Day 20    | Revision for Unit I Test.                                                                           |
| Day 21    | <b>Unit I Test</b> (Covering Riemann integrals, the Fundamental Theorem, and Mean Value Theorems).  |
| Day 22    | Test feedback, discussion of common errors, and remedial practice for Unit I.                       |

### Unit II: Improper Integrals & Integrals as a Function of a Parameter

| Day                    | Topic                                                                                                             |
|------------------------|-------------------------------------------------------------------------------------------------------------------|
| Day 23–25              | Introduction to improper integrals (Type 1 and Type 2) and their convergence with examples.                       |
| Day 26–28              | Comparison tests for convergence of improper integrals (direct, limit, and $\mu$ -test).                          |
| Day 29–31              | Advanced convergence tests: Abel's test and Dirichlet's test with worked examples.                                |
| Day 32–34              | Frullani's integral: Statement, proof, and application problems.                                                  |
| Day 35–37              | Integral as a function of a parameter: Concept and examples.                                                      |
| Day 38–40              | Continuity, differentiability, and integrability of an integral of a function of a parameter.                     |
| Day 41–42              | Intensive problem-solving session covering all topics in Unit II.                                                 |
| Day 43                 | Revision for Unit II Test.                                                                                        |
| Day 44                 | <b>Unit II Test</b> (Covering improper integrals, convergence tests, and integrals as a function of a parameter). |
| Continued on next page |                                                                                                                   |

| Day    | Topic                                            |
|--------|--------------------------------------------------|
| Day 45 | Test feedback and remedial practice for Unit II. |

## Unit III: Metric Spaces I

| Day       | Topic                                                                                     |
|-----------|-------------------------------------------------------------------------------------------|
| Day 46–48 | Definition and examples of metric spaces; pseudo-metrics and equivalent metrics.          |
| Day 49–51 | Neighborhoods, limit points, interior points, and their properties.                       |
| Day 52–54 | Open sets, closed sets, closure, interior, and boundary of a set.                         |
| Day 55–57 | Subspace of a metric space with examples.                                                 |
| Day 58–60 | Cauchy sequences and the concept of completeness in metric spaces.                        |
| Day 61–63 | Cantor's intersection theorem and Baire's category theorem with proofs.                   |
| Day 64–65 | The Contraction Principle (Banach fixed-point theorem) and its applications.              |
| Day 66    | Problem-solving session and revision for Unit III.                                        |
| Day 67    | <b>Unit III Test</b> (Covering basic metric space topology, sequences, and completeness). |
| Day 68    | Test feedback and remedial practice for Unit III.                                         |

## Unit IV: Metric Spaces II

| Day       | Topic                                                                                                       |
|-----------|-------------------------------------------------------------------------------------------------------------|
| Day 69–71 | Continuous functions in metric spaces: Definitions ( $\varepsilon$ - $\delta$ and sequential) and examples. |
| Day 72–74 | Uniform continuity: Definition, examples, and relationship with continuity.                                 |
| Day 75–77 | Compactness for metric spaces: Definitions, sequential compactness, and the Bolzano-Weierstrass property.   |
| Day 78–80 | Total boundedness and the finite intersection property.                                                     |
| Day 81–83 | Continuity in relation to compactness.                                                                      |
| Day 84–86 | Connectedness: Definitions, components, and continuity in relation to connectedness.                        |
| Day 87–88 | Mixed problem-solving session (Units III & IV) and comprehensive revision.                                  |
| Day 89    | Final revision and doubt-clearing session.                                                                  |
| Day 90    | <b>Final Theory Test</b> (Comprehensive; covers Units I-IV).                                                |

# Groups and Rings Lesson Plan (Paper: 12BSM 352)

## Unit I: Introduction to Groups

| Day       | Topic                                                                                         |
|-----------|-----------------------------------------------------------------------------------------------|
| Day 1     | Course introduction, syllabus overview, and assessment pattern.                               |
| Day 2–4   | Definition of a group, abelian groups, finite and infinite groups, and simple properties.     |
| Day 5–7   | Subgroups: Definition, examples, and subgroup criteria.                                       |
| Day 8–10  | Generation of groups and the concept of cyclic groups, with properties and theorems.          |
| Day 11–13 | Cosets: Left and right cosets, their properties, and index of a subgroup.                     |
| Day 14–16 | Coset decomposition and Lagrange's theorem with its consequences.                             |
| Day 17–19 | Normal subgroups: Definition, criteria, and examples.                                         |
| Day 20    | Quotient groups: Definition, construction, and related theorems.                              |
| Day 21    | <b>Unit I Test</b> (Covering groups, subgroups, cyclic groups, cosets, and normal subgroups). |
| Day 22    | Test feedback, discussion of common errors, and remedial practice for Unit I.                 |

## Unit II: Homomorphisms and Permutation Groups

| Day       | Topic                                                                                |
|-----------|--------------------------------------------------------------------------------------|
| Day 23–26 | Homomorphisms of groups: Definition, examples, kernel, and image.                    |
| Day 27–29 | Isomorphisms, automorphisms, and inner automorphisms of a group.                     |
| Day 30–32 | Automorphisms of cyclic groups with proofs and examples.                             |
| Day 33–35 | Permutation groups: Symmetric groups, cycles, and transpositions.                    |
| Day 36–38 | Even and odd permutations and the alternating group ( $A_n$ ).                       |
| Day 39–41 | Cayley's theorem: Statement, proof, and significance.                                |
| Day 42    | Center of a group and the derived group of a group.                                  |
| Day 43    | Problem-solving session and revision for Unit II.                                    |
| Day 44    | <b>Unit II Test</b> (Covering homomorphisms, automorphisms, and permutation groups). |
| Day 45    | Test feedback and remedial practice for Unit II.                                     |

## Unit III: Introduction to Rings

| Day       | Topic                                                                             |
|-----------|-----------------------------------------------------------------------------------|
| Day 46–49 | Introduction to rings: Definition, types (commutative, with unity), and examples. |
| Day 50–52 | Subrings: Definition, criteria, and examples.                                     |
| Day 53–56 | Integral domains and fields: Definitions, properties, and examples.               |

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| Day       | Topic                                                                                       |
|-----------|---------------------------------------------------------------------------------------------|
| Day 57–59 | Characteristics of a ring with examples.                                                    |
| Day 60–62 | Ring homomorphisms: Definition, properties, kernel, and image.                              |
| Day 63–65 | Ideals: Definition, types (principal, prime, maximal), and their properties.                |
| Day 66    | Quotient rings and the field of quotients of an integral domain.                            |
| Day 67    | <b>Unit III Test</b> (Covering rings, integral domains, fields, ideals, and homomorphisms). |
| Day 68    | Test feedback and remedial practice for Unit III.                                           |

## Unit IV: Special Rings and Polynomials

| Day       | Topic                                                                                                |
|-----------|------------------------------------------------------------------------------------------------------|
| Day       | Topic                                                                                                |
| Day 69–72 | Euclidean rings (Euclidean domains): Definition, properties, and examples ( $\mathbb{Z}$ , $F[x]$ ). |
| Day 73–76 | Introduction to polynomial rings and their basic properties.                                         |
| Day 77–79 | Polynomials over the rational field and the Eisenstein's criterion for irreducibility.               |
| Day 80–82 | Polynomial rings over commutative rings.                                                             |
| Day 83–86 | Unique Factorization Domain (UFD): Definition and properties.                                        |
| Day 87    | Theorem: If $R$ is a UFD, then $R[x_1, x_2, \dots, x_n]$ is also a UFD.                              |
| Day 88    | Mixed problem-solving session and comprehensive revision for all units.                              |
| Day 89    | Final revision and doubt-clearing session.                                                           |
| Day 90    | <b>Final Theory Test</b> (Comprehensive; covers Units I-IV).                                         |

### Lesson Plan 2025-26

Name of the Assistant Professor: **Ms. Manisha**

Class and Section: **B.Sc. 5<sup>th</sup> Semester**

Subject: **Mathematics (Numerical Analysis)**

| Week | Date              | Topics                                                                                                                                                                                            |
|------|-------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1    | 1 Aug- 9Aug       | Introduction to finite difference operators, forward difference, backward difference, fundamental theorem of difference calculus, properties of operators, difference of some functions.          |
| 2    | 11 Aug- 16 Aug    | Displacement or shift operators and its properties, relation between various operators, exercise 1.1, error in tabular value, exercise 1.2.                                                       |
| 3    | 18 Aug – 23 Aug   | Introduction to interpolation, Newton's formula for forward interpolation, Newton backward interpolation formula, exercise 2.1, subdivision of intervals, exercise 2.2                            |
| 4    | 25 Aug – 30 Aug   | Newton's divided difference formula, exercise 3.1, lagrange's interpolation formula, Hermite's interpolation formula, exercise 3.2.                                                               |
| 5    | 1 Sept – 6 Sept   | Gauss forward interpolation formula, Gauss backward interpolation formula, Sterling formula, Bessel's formula, exercise 4.1.                                                                      |
| 6    | 8 Sept – 13 Sept  | Introduction to probability distribution, random variable, mean and variance of a random variable, binomial distribution, Recurrence formula, fitting a binomial distribution, exercise 5.1, 5.2. |
| 7    | 15 Sept – 20 Sept | Poisson distribution, normal distribution, exercise 5.3, 5.4, Introduction to numerical differentiation.                                                                                          |
| 8    | 22 Sept – 27 Sept | Numerical distribution using Newton forward, Newton backward, Sterling formula, exercise 6.1.                                                                                                     |
| 9    | 29 Sept – 4 Oct   | Eigen values, eigen vectors, Power method, Jacobi's method for symmetric matrix, Tridiagonal matrix.                                                                                              |

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| 10 | 6 Oct – 11 Oct  | Given's method, House holder method, exercise 7.1, QR method, Lancos's method.                                                                                                                                       |
| 11 | 13 Oct – 18 Oct | Numerical integration, Newton-Cotes quadrature formula, Trapezoidal rule, Simpson's one-third rule, Simpson's three-eighth rule, error in quadrature formulae.                                                       |
| 12 | 27 Oct- 1 Nov   | Gauss's quadrature formula, exercise 8.1. Introduction to numerical solution of ODE, Single step and multiple step method, Euler's method, Euler's modified method, exercise 9.1, Taylor's series method, RK Method. |
| 13 | 03 Nov- 08 Nov  | Picard's Method, exercise 9.2, predictor corrector method: Milne- Simpson's Method, Adam-Bashforth method, exercise 9.3.                                                                                             |
| 14 | 10 Nov- 15 Nov  | Program of Newton forward, Newton backward interpolation formula, Lagrange's interpolation.                                                                                                                          |
| 15 | 17 Nov- 22 Nov  | Program of Trapezoidal rule, Simpson's one-third rule, Simpson's three-eighth rule, Euler's Method, Euler's Modified method.                                                                                         |
| 16 | 24 Nov- 29 Nov  | Problem Discussion, Revision                                                                                                                                                                                         |
| 17 | 1 Dec onwards   | EXAMINATIONS                                                                                                                                                                                                         |